# 6. MATHEMATICS

### B.Sc. Part-II 2020

Teaching: 3 Hours per Week per Theory Paper.

2 Hours per Week per Batch for Practical

#### **Examination Scheme:**

	Min.Pass Marks		Max. Marks
	Science – 54 Arts – 72		150 200
Paper – I	Real Analysis	Duration 3 hrs.	Max. Marks 40 (Science) 53 (Arts)
Paper – II	Differential Equations	3 hrs.	40 (Science) 53 (Arts)
Paper – III	Numerical Analysis	3 hrs.	40 (Science) 54 (Arts)
Practical		2 hrs.	30 (Science) 40 (Arts)

#### Note:

- 1. Common paper will be set for both the Faculties of Social Science and Science. However, the marks obtained by the candidate in the case of Faculty of Social Science will be converted according to the ratio of the maximum marks of the papers in the two Faculties.
- 2. Each candidate is required to appear in the Practical examination to be conducted by internal and external examiners. External examiner will be appointed by the University and internal examiner will be appointed by the Principal in consultation with Local Head/Head, Department of Mathematics in the college.
- 3. An Internal/external examiner can conduct Practical Examination of not more than 100 (Hundred) Candidates.
- 4. Each candidate has to pass in Theory and Practical examinations separately.

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# Paper - I: Real Analysis

Teaching: 3 Hours per Week

**Duration of Examination: 3 Hours** 

Max. Marks:

40 (Science)

53 (Arts)

Note: This paper is divided into FIVE Units. TWO questions will be set from each Unit. Candidates are required to attempt FIVE questions in all taking ONE question from each Unit. All questions carry equal marks.

Unit 1: Real numbers as complete ordered field, Limit point, Bolzano-Weierstrass theorem, closed and Open sets. Concept of compactness and connectedness. Heine-Borel theorem. Holder inequality & Minkowski inequality, Metric space — Definition and examples, Open and Closed sets, Interior and Closure of a set, Limit point of a set in metric space.

Unit 2: Real sequences- Limit and Convergence of a sequence, Monotonic sequences. Cauchy's sequences, Subsequences, Cauchy's general principle of convergence. Properties of continuous functions on closed intervals.

Unit 3: Properties of derivable functions, Darboux's and Rolle's theorem. Notion of limit, continuity and differentiability for functions of several variables. The directional derivative, the total derivative, expression of total derivative in terms of partial derivatives.

Unit 4: Riemann integration – Lower and Upper Riemann integrals, Riemann integrability, Mean value theorem of integral calculus, Fundamental theorem of integral calculus. Functions of bounded variations. Introduction, properties of functions of bounded variations, total variation.

Unit 5: Sequence and series of functions – Pointwise and Uniform convergence, Cauchy's criterion, Weierstrass M-test, Abel's test, Dirichlet's test for uniform convergence of series of functions, Uniform convergence and Continuity of series of functions, Term by term differentiation and integration.

### Reference Books:

- 1. K.A. Ross, Elementary Analysis: The Theory of Calculus, Undergraduate Texts in Mathematics, Springer (SIE), Indian reprint, 2004.
- 2. R.G. Bartle D.R. Sherbert, Introduction to Real Analysis (3rd edition), John Wiley and Sons (Asia) Pvt. Ltd.., Singapore, 2002.
- 3. Charles G. Denlinger, Elements of Real Analysis, Jones and Bartlett (Student Edition),2011.
- 4. S. Kumaresan, Topology of Metric Spaces, Narosa Publishing House, Second Edition 2011.
- 5. G. F. Simmons, Introduction to Topology and Modern Analysis, Mcgraw-Hill, Edition 2004.

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# Paper - II: Differential Equations

Teaching: 3 Hours per Week

**Duration of Examination: 3 Hours** 

Max. Marks:

40 (Science)

53 (Arts)

Note: This paper is divided into FIVE Units. TWO questions will be set from each Unit. Candidates are required to attempt FIVE questions in all taking ONE question from each Unit. All questions carry equal marks.

Unit 1: Degree and order of a differential equation. Equations of first order and first degree. Equations in which the variables are separable. Homogeneous equations and equations reducible to homogeneous form. Linear equations and equations reducible to linear form. Exact differential equations and equations which can be made exact.

Unit 2: First order but higher degree differential equations solvable for x,y and p. Clairaut's form and singular solutions with Extraneous Loci. Linear differential equations with constant coefficients, Complimentary function and Particular integral.

Unit 3: Homogeneous linear differential equations, Simultaneous differential equations. Exact linear differential equations of nth order. Existence and uniqueness theorem.

Unit 4: Linear differential equations of second order. Linear independence of solutions. Solution by transformation of the equation by changing the dependent variable/the independent variable, Factorization of operators, Method of variation of parameters, Method of undetermined coefficients.

Unit 5: Partial differential equations of the first order. Lagrange's linear equation. Charpit's general method of solution. Homogeneous and non-homogeneous linear partial differential equations with constant coefficients. Equations reducible to equations with constant coefficients.

## Reference Books:

- 1. R.S. Senger, Ordinary Differential Equations with Integration, Prayal Publ. 2000.
- 2. D.A. Murray, Introductory Course in Differential Equations, Orient Longman (India), 1967.
- 3. E.A. Codington, An Introduction to Ordinary Differential Equations, Prentice Hall of India, 1961.

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# Paper - III: Numerical Analysis and Vector Calculus

Teaching: 3 Hours per Week

**Duration of Examination: 3 Hours** 

Max. Marks:

40 (Science)

54 (Arts)

Note: (i) This paper is divided into FIVE Units. TWO questions will be set from each Unit. Candidates are required to attempt FIVE questions in all taking ONE question from each Unit. All questions carry equal marks.

(ii) Non-Programmable Scientific Calculators are allowed.

Unit 1: Differences. Relation between differences and derivatives. Differences of a polynomial. Newton's formulae for forward and backward interpolation. Divided differences. Newton's divided difference, Lagrange's interpolation formula.

Unit 2: Central differences. Gauss's, Stirling's and Bessel's interpolation formulae. Numerical Differentiation. Derivatives from interpolation formulae. Numerical integration, Derivations of general quadrature formulas, Trapazoidal rule. Simpson's one-third, Simpson's three-eighth and Gauss's quadrature formulae.

Unit 3: Relation between the roots and coefficients of general polynomial equation in one variable, transformation of equations, Descarte's rule of signs, solution of cubic equations by Cardon's method, biquadratic equations by Ferari's method.

Numerical solution of Algebraic and Transcendental equations, Bisection method, Secant method, Regula-Falsi method, Iteration method, Newton- Raphson Method (derivation of formulae and rate of convergence only).

Unit 4: Gauss elimination and Iterative methods (Jacobi and Gauss Seidal) for solving system of linear algebraic equations. Partial Pivoting method, ill conditioned systems, Numerical solutions of ordinary differential equations of first order with initial condition using Picard's, Euler and modified Euler's method.

Unit 5: Scalar and Vector point functions. Differentiation and integration of vector point functions. Directional derivative. Differential operators. Gradient, Divergence and Curl. Theorems of Gauss, Green, Stokes (without proof) and problems based on these theorems.

## Reference Books:

- 1. B. Bradie, A Friendly Introduction to Numerical Analysis, Pearson Education, India, 2007.
- C. F. Gerald and P. O. Wheatley, App;ied Numerical Analysis, Pearson Education, India,7th edition, 2008.
- 3. C.F. Gerald, P.O. Wheatley, Applied Numerical Analysis, Addison-Wesley, 1998.

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#### Practical

Teaching: 2 hours per week per batch not more than 20 students.

<b>Examination Scheme:</b>			<b>Duration: 2 Hours</b>
	Science	Arts	
Max.Marks	30	40	
Min.Pass Marks	11	15	
Distribution of Marks:			

Two Practicals one from each group

10 Marks each	=	20 Marks	(13 Marks each) 26
Practical Record	==	05 Marks	07
Viva-voce	=	05 Marks	07
Total Marks	<del>=</del>	30 Marks	40

The paper will contain TWO practical. The candidates are required to attempt both practical.

Practicals with Computer Programming in C Language.

Programming languages and problem solving on computers, Algorithm, Flow chart, Programming in C- Constants, Variables, Arithmetic and logical expressions, Input-Output, Conditional statements, Implementing loops in Programs, Defining and manipulation arrays and functions.

#### Group A:

- 1. Printing n terms of Fibonacci sequence.
- 2. Finding n!,  $\sum n$ ,  $\sum n^2$  etc.
- 3. Defining a function and finding sum of n terms of a series/sequence whose general term is given (e.g.  $a_n = \frac{n^2+3}{n+1}$ ).
- 4. Printing Pascal's triangle.
- 5. Finding gcd and lcm of two numbers by Euclid's algorithm.
- 6. Checking prime/composite number.
- 7. Finding number of primes less than  $n, n \in \mathbb{Z}$ .
- 8. Finding mean, standard deviation and  ${}^{n}P_{r}$ ,  ${}^{n}C_{r}$  for different n and r.

## Group B:

1. Numerical integration using Trapezoidal, Simpson's 1/3, 3/8 and Waddle rules.

#### Note:

- 1. Each Candidate (Regular/non-Collegiate) has to prepare his/her practical record.
- 2. Each Candidate has to pass in Practical and Theory examinations separately.

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